

## MATH 541, FALL 2023, HOMEWORK 11

Due Saturday, December 2, 2023 at 5pm Eastern time on Gradescope. Solve the following exercises:

**Problem 1.** Lawler, exercise 8.4. You should briefly justify each answer.

**Problem 2.** Lawler, exercise 8.9.

**Problem 3.** Lawler, exercise 8.11.

**Problem 4.** Lawler, exercise 8.15.

**Problem 5.** Let  $p_t(x, y)$  be the transition probability density for Brownian motion

$$p_t(x, y) = \frac{1}{\sqrt{2\pi t}} \exp\left\{-\frac{(y-x)^2}{2t}\right\}.$$

Check explicitly that

$$\frac{\partial}{\partial t} p_t(x, y) = \frac{1}{2} \frac{\partial^2}{\partial y^2} p_t(x, y).$$