Everything you'll need to know is on the master website:

http://people.math.gatech.edu/~cjankowski3/teaching/f2017/m1553/index.html

or on the website for this section:

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http://people.math.gatech.edu/~jrabinoff/1718F-1553/
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(There is a link from T-Square.) **Read them! Bookmark them!** Chances are, all your (non-math) questions are answered there.

- ▶ Warmup assignment is due on Friday at 11:59pm on WeBWorK.
- Enroll in Piazza (the link is on T-Square). You can ask questions there, and we will use it for in-class polling on a daily basis. Please use your T-Square email address to enroll, so that your poll responses show up in the T-Square gradebook. Please join the Piazza group "1553-A and C".
- It's probably easiest to respond to polls using a smartphone. Download the Piazza app.
- My office is Skiles 244 and my office hours are Monday, 1–3pm and Tuesday, 9–11am.
- Your TAs have office hours too. You can go to any of them. Details on the website.

Chapter 1

Linear Equations

Recall that **R** denotes the collection of all real numbers, i.e. the number line. It contains numbers like $0, -1, \pi, \frac{3}{2}, \ldots$

Definition

Let n be a positive whole number. We define

 \mathbf{R}^n = all ordered *n*-tuples of real numbers $(x_1, x_2, x_3, \dots, x_n)$.

Example

When n = 1, we just get **R** back: $\mathbf{R}^1 = \mathbf{R}$. Geometrically, this is the *number* line.

Example

When n = 2, we can think of \mathbf{R}^2 as the *plane*. This is because every point on the plane can be represented by an ordered pair of real numbers, namely, its *x*-and *y*-coordinates.



We can use the elements of ${\bf R}^2$ to *label* points on the plane, but ${\bf R}^2$ is not defined to be the plane!

Example

When n = 3, we can think of \mathbf{R}^3 as the *space* we (appear to) live in. This is because every point in space can be represented by an ordered triple of real numbers, namely, its *x*-, *y*-, and *z*-coordinates.



Again, we can use the elements of \mathbf{R}^3 to *label* points in space, but \mathbf{R}^3 is not defined to be space!

Example

All colors you can see can be described by three quantities: the amount of red, green, and blue light in that color. So we could also think of \mathbb{R}^3 as the space of all *colors*:



Again, we can use the elements of \mathbf{R}^3 to *label* the colors, but \mathbf{R}^3 is not defined to be the space of all colors!

So what is \mathbf{R}^4 ? or \mathbf{R}^5 ? or \mathbf{R}^n ?

... go back to the *definition*: ordered *n*-tuples of real numbers

$$(x_1, x_2, x_3, \ldots, x_n).$$

They're still "geometric" spaces, in the sense that our intuition for \mathbf{R}^2 and \mathbf{R}^3 sometimes extends to \mathbf{R}^n , but they're harder to visualize.

Last time we could have used \mathbf{R}^4 to label the amount of traffic (x, y, z, w) passing through four streets.



We'll make definitions and state theorems that apply to any \mathbf{R}^n , but we'll only draw pictures for \mathbf{R}^2 and \mathbf{R}^3 .

Section 1.1

Systems of Linear Equations

One Linear Equation

What does the solution set of a linear equation look like?

x + y = 1 where y = 1 - xThis is called the **implicit equation** of the line.

We can write the same line in parametric form in ${\bf R}^2$:

(x, y) = (t, 1-t) t in **R**.

This means that every point on the line has the form (t, 1 - t) for some real number t.





Aside

What is a line? A ray that is *straight* and infinite in both directions.

What does the solution set of a linear equation look like? x + y + z = 1 where x +

Does this plane have a parametric form?

$$(x, y, z) = (t, w, 1 - t - w)$$
 $t, w \text{ in } \mathbf{R}.$

Note: we are *labeling* the points on the plane by elements (t, w) in \mathbb{R}^2 .

Aside

What is a plane? A flat sheet of paper that's infinite in all directions.

One Linear Equation

What does the solution set of a linear equation look like?

x + y + z + w = 1 where x + y + z + w = 1 a "3-plane" in "4-space"... [not pictured here]

Everybody get out your gadgets!

Systems of Linear Equations

What does the solution set of a *system* of more than one linear equation look like?





In general it's an intersection of lines, planes, etc.

[two planes intersecting]

Kinds of Solution Sets

In what other ways can two lines intersect?

x - 3y = -3x - 3y = 3



A system of equations with no solutions is called inconsistent.

Kinds of Solution Sets

In what other ways can two lines intersect?

 $\begin{aligned} x - 3y &= -3\\ 2x - 6y &= -6 \end{aligned}$



Note that multiplying an equation by a nonzero number gives the *same* solution set. In other words, they are *equivalent* (systems of) equations.

What about in three variables?